## **Listing of the Claims**

This listing of the claims will replace all prior versions, and listings, of claims in the Application:

1. (Original) A method for determining vibration amplitude limits to detect faults in mechanical equipment, comprising:

estimating a data probability distribution based on data for the mechanical equipment; and

utilizing the data probability distribution to calculate the vibration amplitude limits.

- 2. (Original) The method of Claim 1 further comprising removing outlier data.
- 3. (Currently Amended) The method of Claim 2 further comprising A method for determining vibration amplitude limits to detect faults in mechanical equipment, comprising:

estimating a data probability distribution based on data for the mechanical equipment;

utilizing the data probability distribution to calculate the vibration amplitude limits;

removing outlier data; and

calculating the vibration amplitude limits as a function of frequency for a substantial portion of the frequency spectrum.

- 4. (Currently Amended) The method of Claim 3 [[1]] wherein the data probability distribution is calculated using statistics and historical data of the mechanical equipment.
- 5. (Original) The method of Claim 4 further comprising specifying importance levels for certain frequencies.

- 6. (Original) The method of Claim 5 wherein the certain frequencies comprise frequencies for at least one of a motor, a compressor, or a gear.
- 7. (Original) The method of Claim 6 further comprising obtaining vibration spectra comprising individual spectrum for the mechanical equipment from a database.
- 8. (Original) The method of Claim 7 further comprising calculating a frequency for the individual spectrum and identifying the individual spectrum having a smallest number of frequency lines.
- 9. (Original) The method of Claim 8 further comprising calculating noise bandwidths and a largest noise bandwidth.
- 10. (Original) The method of Claim 9 further comprising collecting vibration data from all spectra in a given frequency range.
- 11. (Original) The method of Claim 4 wherein the data probability distribution is calculated using a kernel density method.
- 12. (Original) The method of Claim 11 wherein the kernel density method comprises calculating conditional kernel density.
- 13. (Original) The method of Claim 12 wherein calculating conditional kernel density comprises estimating an unknown probability density for a given dataset.

14. (Original) The method of Claim 13 wherein the probability density estimate at a point x for a one-dimensional dataset with n data points is given by:

$$p(x) = \frac{1}{n h} \sum_{j=1}^{n} \kappa \left( \frac{x - x_j}{h} \right)$$

where,  $x_j$  is the  $j^{th}$  observation of dataset X, h is a bandwidth that characterizes a spread of the kernel, and  $\kappa(\cdot)$  is a kernel density function that is symmetric and satisfies the condition:  $\int_{-\infty}^{\infty} \kappa(u) du = 1$ .

- 15. (Original) The method of Claim 14 wherein the kernel density estimate is a two-dimensional kernel density estimate utilizing frequency and amplitude directions of the frequency spectrum.
- 16. (Original) The method of Claim 15 wherein a *d*-dimensional kernel density estimate is generally written as:

$$p(x) = \frac{1}{n} \sum_{j=1}^{n} |H|^{-1/2} K(H^{-1/2}(x - x_j))$$

where K (u) is a d-dimensional kernel, H is a bandwidth matrix, and  $|\cdot|$  denotes a matrix determinant.

- 17. (Original) The method of Claim 4 further comprising detecting one or more faults in the mechanical equipment.
- 18. (Currently Amended) The method of Claim 3 [[1]] wherein the mechanical equipment comprises one or more HVAC chillers.

19. (Original) A method for detecting faults in a chiller based on vibration amplitude limits, comprising:

calculating vibration amplitude limits of the chiller using statistics and historical data for the chiller;

estimating an at least two-dimensional density estimate; and weighting the historical data based on when the historical data was generated;

wherein the vibration amplitude limits are calculated as a function of frequency for an entire frequency spectrum.

- 20. (Original) The method of Claim 19 further comprising removing outlier data.
- 21. (Original) The method of Claim 20 wherein the at least two-dimensional density estimate utilizes frequency and amplitude directions of the frequency spectrum.
- 22. (Original) The method of Claim 21 wherein the at least two-dimensional density estimate is a *d*-dimensional kernel density estimate.
- 23. (Original) The method of Claim 22 wherein the d-dimensional kernel density estimate for point x of a dataset with n data points is given by:

$$p(x) = \frac{1}{n} \sum_{j=1}^{n} |H|^{-1/2} K(H^{-1/2}(x - x_j))$$

where,  $x_j$  is the  $j^{th}$  observation of the dataset, K (u) is a d-dimensional kernel, H is a bandwidth matrix, and  $|\cdot|$  denotes a matrix determinant.

24. (Original) The method of Claim 22 further including obtaining vibration spectra comprising individual spectrum for the chiller from a database.

- 25. (Original) The method of Claim 24 further comprising calculating a frequency for the individual spectrum and identifying an individual spectrum having the smallest number of frequency lines.
- 26. (Original) The method of Claim 25 further comprising calculating noise bandwidths and a largest noise bandwidth.
- 27. (Original) The method of Claim 26 further comprising collecting vibration data from all spectra in a given frequency range.
- 28. (Original) The method of Claim 19 further comprising calculating a conditional kernel density.
- 29. (Original) The method of Claim 28 wherein calculating the conditional kernel density comprises estimating an unknown probability density for a given dataset.
- 30. (Original) A method for determining vibration amplitude limits of a mechanical device comprising:

identifying a mechanical device and a frequency range for a spectrum to be analyzed;

retrieving vibration spectra comprising individual spectrum for the mechanical device and the frequency range;

calculating frequency for the individual spectrum;

identifying the individual spectrum with a smallest number of frequency lines;

calculating noise bandwidths and a largest noise bandwidth;

removing outlier data;

calculating conditional kernel density; and

calculating vibration amplitude limits to detect faults in the mechanical

device.

- 31. (Original) The method of Claim 30 wherein the mechanical device comprises a chiller for an HVAC system.
- 32. (Original) The method of Claim 30 wherein the vibration spectra for the mechanical device and the frequency range is obtained from a database.
- 33. (Original) The method of Claim 32 wherein calculating conditional kernel density comprises estimating an unknown probability density for a given dataset.
- 34. (Original) The method of Claim 33 wherein the probability density estimate at a point x for a one-dimensional dataset with n data points is given by:

$$p(x) = \frac{1}{nh} \sum_{j=1}^{n} \kappa \left( \frac{x - x_j}{h} \right)$$

where,  $x_j$  is the  $j^{th}$  observation of the dataset, h is a bandwidth that characterizes a spread of the kernel, and  $\kappa(\cdot)$  is a kernel density function that is symmetric and satisfies the condition:  $\int_{-\infty}^{\infty} \kappa(u) du = 1.$ 

- 35. (Original) The method of Claim 33 wherein the kernel density estimate is at least a two-dimensional kernel density estimate utilizing frequency and amplitude directions of the frequency spectrum.
- 36. (Original) The method of Claim 35 wherein a *d*-dimensional kernel density estimate is given by:

$$p(x) = \frac{1}{n} \sum_{i=1}^{n} |H|^{-1/2} K(H^{-1/2}(x - x_i))$$

where K (u) is a d-dimensional kernel, H is a bandwidth matrix, and  $|\cdot|$  denotes a matrix determinant.